# A Course Recommender System Based on Graduating Attributes

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Abstract: Assessing learning outcomes for students in higher education institutes is an interesting task with many potential applications for all involved stakeholders (students, administrators, potential employers, etc.). In this paper, we propose a course recommendation system for students based on the assessment of their "graduate attributes" (i.e. attributes that describe the developing values of students). Students rate the improvement in their graduating attributes after a course is finished and a collaborative filtering algorithm is utilized in order to suggest courses that were taken by fellow students and rated in a similar way. An extension to weigh the most recent ratings as more important is included in the algorithm which is shown to have better accuracy than the baseline approach. Experimental results using correlation thresholding and the nearest neighbors approach show that such a recommendation system can be effective when an active neighborhood of 10-15 students is used and show that the numbers of users used can be decreased effectively to one fourth of the whole population for improving the performance of the algorithm.

## **1 INTRODUCTION**

Across institutions of higher education around the world, one of the topics of research that there is much focus on is about ensuring the students achievement of the intended learning outcomes (ILO) set by various programs. These ILOs are linked to "competencies" required within programs to perform specific tasks. Competencies are the ability to do something successfully or efficiently [Oxford dictionary]. Within academia, competencies are "multidimensional construct composed of the skills, attitudes, and behaviors of a learner that contribute to academic success in the classroom" (DiPerna and Elliott, 1999). It is not necessarily limited to classroom, it encloses programs and the whole university experience. When it touches on the latter, these competences lead to attributes that are linked directly to the overall vision and mission of a specific institution.

The University of Alberta's provost office in 2011, undertook a task of identifying its 7 graduate attributes with their 28 sub-attributes (Provost office, 2011). These are proposed to describe the qualities, values and dispositions that students are develop during their time at the university. Graduate Attributes have been taking momentum since the early 20th century. One of the most commonly used definitions of Graduating attributes (GAs) suggested by Bowden et al. says:

"Graduate attributes are the qualities, skills and understandings a university community agrees its students should develop during their time with the institution. These attributes include but go beyond the disciplinary expertise or technical knowledge that has traditionally formed the core of most university courses. They are qualities that also prepare graduates as agents of social good in an unknown future." (Bowden et al., 2000)

In the last two decades, universities have identified their respective GAs, but ensuring that actually the acquisition of GAs does happen, has been elusive. Ipperciel and ElAtia proposed a dynamic model for assessing the GAs (Ipperciel and ElAtia, 2014). This model is based on rubrics that are linked to can-do statement where they introduced a 1 to 5 likert scales for assessing each of the Graduate Attributes and their sub-attributes. The 5 levels scale range from emergent, basic, adequate, superior to exceptional. This model of assessment is based on an interaction from teachers and students with specific courses and their ILOs. The model allows students and teachers to carry out self-assessment based on their own experience and interaction with course materials. For the students part, as the assessment progresses, they are

providing more input and the model adjusts to their profiles using the background survey that they initially fill. The model for the assessment of the GAs is longitudinal and is built upon the following triangulation: awareness, motivation and engagement.

In our work, we have adopted this assessment model of GAs and designed within it a recommender system that would use the data supplied by the students and would recommend courses to students based on their self-assessment. Although we have implemented a platform for gathering the data needed, we were not able to gather sufficient amount of data for the evaluation of a course recommender system. As a result, for training and testing our model we needed to generate synthetic data based on the expected structure of data. We will use this synthetic data for training and evaluation of our course recommender system.

In this paper, we are describing how the assessment of the GAs can be used to generate course recommendation. The overall goal of the system is to recommend to students courses that will improve either their average competence profile or specific competences that students would target, for instance, what courses are recommended for a student in engineering to take if s/he want to go from an adequate level to a superior level in critical thinking. The algorithm relies on assessments date provided by the students and works in a collaborative filtering context taking into account the time factor (i.e. recent student assessments add more value to the recommendation).

The rest of the paper is organized as follows: Section 2 presents related work in the field. Data used in the current paper as well as the algorithm framework of recommendation are presented in Section 3. Experiments are described in Section 4 and finally Section 5 concludes the paper and presents future work directions.

# 2 RELATED WORK

There have been many data mining systems developed in education (Romero and Ventura, 2010) and especially on how recommender systems can be utilized for suggesting courses (O'Mahony and Smyth, 2007) or master programs (Surpatean et al., 2012). Most of them use only the actual course content or the curriculum connections (Lee and Cho, 2011) or the performance of students based on their grades (Goga et al., 2015) or past selections of student courses (Chu et al., 2003) but there is no research work on suggesting courses based on the developing attributes of students. Such a direction would require to go beyond the traditional recommendation representation of *users* × *ratings* and adopt a "multicriteria rating" approach (Adomavicius and Tuzhilin, 2005). In this direction, there have only been a few attempts in the course recommendation concept (Le Roux et al., 2007) but none takes into account graduating attributes.

Finally, new approaches have emerged that take into account the dynamical nature of ratings data (i.e. introduce the time dimension) (Vinagre, ), which is also a direction not yet studied in educational systems. Given the fact that educational data are also spread across different time units (e.g. semesters, years, etc.), a direction that would assign decreasing weights to older data (Ding and Li, 2005) would provide more accurate results.

Our approach in this paper introduces a timeaware course recommendation system based on the graduating attributes of students (and is not based on the course content or students' grades) and provides interesting avenues for future work.

### **3** ALGORITHM DESCRIPTION

#### **3.1** Data generation

There can be various ways for gathering data regarding the graduating attributes. One way is by selfassessment of students in each semester. In this selfassessment, students can report the courses they recognize impactfull in improving their GAs. These impacts then can be used as ratings in the context of recommender systems. In case of not having a selfassessment for GAs and courses, we can recognize the impact-full attributes of each course by the instructor's assessment, and then use the performance of student's as a rating for all the attributes.

The tool for collecting data based on the scenario of self-assessment has been implemented at the University of Alberta; however, data collection for the purpose of training and testing of a recommender system may need years to accomplish. In this paper we have generated synthetic data based on the scenario of using self-assessment and the implemented tool. For the purpose of data generation, we first need to recognize the list of attributes which will be assessed (rated) and the values which can be assigned to each of the attributes. In our tool we have 28 sub-attributes which can be assessed by student by assigning a value between 1 and 5 to each of them. We have used the same numbers for our synthetic data. We have also simulated the list of courses which will be available for the students. Each of the courses would be described by instructors in terms of GAs, meaning by which degrees each attribute will be improved. Each student will also be described by the list of values assigned to the GAs. In each semester each student will participate in some of the existing courses and those courses will improve the values of attributes. Based on how impactfull the course have been in increasing the value of each attribute the student will rate it. By having these data our application will generate recommendation for courses in the next semesters.

To generate realistic data for the use of our applications, we need to consider how the real data would look like. We have formulated the following list of assumptions and we have considered them in our data synthesis. The list of assumptions we have used is as follows:

- Students may start with different values for attributes as a baseline (they may not be similar), so we can not start all from the lowest value for all attributes. The random value assigned to each attribute for each student is independent of other values.
- Personality of students is a factor in the assessment of competencies (some may report most of the courses as major impact and some the opposite). Students' capacity of learning each attribute is also different from other attributes. Students' personality is independent and constant over time.
- The probability of values assigned to Graduating attributes for each course is not uniform. It is more likely to have lower values compared to higher values.
- In the updating of the values of competencies, all the courses taken in the semester have impact. We assume that the students spend equal time on each course, so we sum the impact of all courses and we divide it by the number of courses.
- The number of courses taken by a student in each semester is not constant. We have assumed that students will take randomly between 4 to 6 courses per semester.

For this study we have assumed having 100 students, 100 courses and 28 attributes (competences). Each of the attributes can have a value between 1 and 5. Each course needs a list of values to describe the amount of focus on each of the attributes ( $C_{kj}$ ). As we are assuming that it is more likely to have lower values compared to higher values in each course; each value has been assigned randomly with more focus on lower values based on Figure 1. As a result, probability of a value being between 1 and 2 has about 7% more chance than being between 2 and 3.

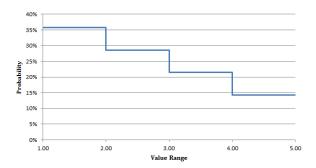


Figure 1: Probability of values assigned to each attribute of each courses

Also we have assigned a uniform random value between 1 and 3 to each attribute of each student as the baseline of student. This way we are considering the different backgrounds of students assuming that no student will start having the highest value which is between 4 and 5. In order to simulate different personalities of students in our data, we have assigned some other factors to each student which based on those we would create the rest of the data. Each student has a talent ratio for each of the attributes, meaning that different students may have different learning potential in regard to each of the attributes  $(T_{ij})$ . Also students may act differently in terms of rating their courses. The rating in our synthesized data is rather 0, 1 or 2 (no impact, minor impact and major impact). Some of the students may rate small changes as 1 but some others may start giving the rating of 1 to bigger changes. As a result for each student we have assigned two limits between 0 and 1 to determine what are the limits of their rating ( $0 < l_{i1} < l_{i2} < 1$ ). If the impact of each course on a competency is between 0 and 1, each user *i* will rate it 0 if it is less than  $l_{i1}$ , 1 if it is between  $l_{i1}$  and  $l_{i2}$  and 2 if it is more than  $l_{i2}$ . Using these values which represent the rating personality of each student we create the rest of the data. We should also mention that the values used for representing the personality of students are independent of each other.

In each semester, students take 4 to 6 courses randomly from all the courses they have not taken before. The new value assigned to each attribute for each student at the end of each semester is calculated with equation 1. As a result each of the courses has some specific impact, and by comparing that impact with the  $l_{i1}$  and  $l_{i2}$  we create the students' ratings. Figure 2 shows the increase of the value assigned to an attribute for different students over time. This can show that students start with different values and the value increases differently for each student over time. For example student 56 has started the first semester with

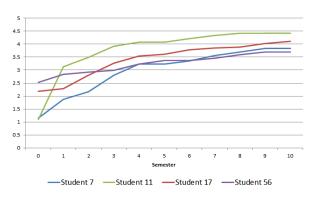


Figure 2: Values assigned to an example attribute over time for some example students in the generated data

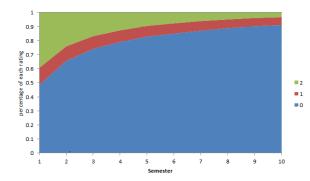


Figure 3: Average ratio of ratings for all student over time

one of the highest values (2.5) compared to other students, but has improved the value with a low pace and has the value of 3.7 by the last semester. On the other hand student 11 has started with value 1.2 but has the value of 4.4 by the last semester.

$$B_{ijt} = B_{ijt-1} + \sum_{k=1}^{K} \frac{\max(0, C_{kj} - B_{ijt-1})T_{ij}}{K}$$
(1)

- *B<sub>ijt</sub>* represents the value assigned to attribute j for student i in semester t
- $C_{ki}$  represents the focus of course k on attribute j
- *T<sub>ij</sub>* represents the talent ratio of student *i* for attribute *j*
- K represents the number of courses for student i

The increase over the values of attributes for each student also results into lower rating in the latest semester as there would be fewer courses to increase those values. Figure 3 shows the ratio of different rates in each semester. Over time the average number of 0 ratings increases and at the same time the average number of 2 ratings decreases.

#### 3.2 Algorithm Design

We first describe the utility of a classic Collaborative Filtering (CF) method. By this term we refer to the algorithm that bases its predictions on neighbours of relevant users. The idea of CF methods lies on the fact that people who agreed in their evaluations for past items are likely to agree again for future items (Resnick et al., 1994).

As for the format we use, each student is represented by a long vector of the courses taken and the assessments (ratings) in regard to the increase in their achieved personal Graduating Attributes (GAs). Similarly, each course is represented by a baseline (ground truth) for the degree that student competences are supposed to increase after the course is taken. One variation in our method of formatting the problem with other applications of CF, is that each rating is given to one aspect (GA) of the course. This can also be considered as "Multicriteria Ratings" in which there exist multiple rating for each criteria of the item (Adomavicius and Tuzhilin, 2005). In this paper we are considering each criteria (GA) of the course as an item. As a result, each item is a pair of Graduating Attribute and a course. This way we can not only recommend a course to a student considering most increase in all GAs, but also recommend a course only targeted on a specific GA. In a hypothetical example of C = 11 courses (cid = 0, 1, ..., 10), S = 5 students (sid = 0, 1, ..., 4) and G = 4 competences (gid = 0, 1, 3), the matrix representation of the problem would look like Table 1.

From Table 1 we see that student 0 (*sid* = 0) has already taken (and rated) 6 courses (*cid* = 0, 1, 2, 3, 4, 5) but has not taken the rest of the courses, so our task would be to recommend courses that this student could take in order either to increase his/her GAs in general (on average) or to increase a specific GA. These recommendations should take into account ratings of similar students to student 0 (collaborative filtering approach).

The CF algorithm utilizes the  $C \times (G \times S)$  matrix (say *R*), like the one in Table 1. The first step is to declare a similarity measure between students in the matrix *R*. The similarity metric based on previous findings (Breese et al., 1998) is chosen to be Pearson Correlation and is provided by the Equation 2 for any two students *a* and *b*.

$$sim(a,b) = \frac{\sum_{g \in G_a \cap G_b} (R_{a,g} - \tilde{R}_a) \cdot (R_{b,g} - \tilde{R}_b)}{\sqrt{\sum_{g \in G_a \cap G_b} (R_{a,g} - \tilde{R}_a)^2} \cdot \sqrt{\sum_{g \in G_a \cap G_b} (R_{b,g} - \tilde{R}_b)^2}} (2)$$
  
where:

	sid=0				sid=1				sid=2				sid=3				sid=4			
cid	g0	g1	g2	g3																
0	0	0	0	1	1	0	1	0	0	0	0	2					2	0	2	2
1	0	1	0	0					0	0	2	0					0	0	2	2
2	0	0	1	0	0	0	0	2	0	2	2	1	0	1	0	0	0	2	0	2
3	0	0	0	2					0	0	0	2	0	0	0	1	2	0	2	0
4	0	2	0	0	0	2	0	0	0	2	2	0	1	0	0	0				
5	1	0	0	0									0	2	0	0				
6	?	?	?	?					0	0	0	2	0	2	1	0	0	1	2	0
7	?	?	?	?					0	2	0	0					0	0	0	2
8	?	?	?	?	0	1	0	0	0	0	2	2					0	0	2	0
9	?	?	?	?					0	1	0	0	0	2	0	1	0	2	2	1
10	?	?	?	?	0	2	1	0	2	0	0	0	2	2	2	0	0	0	0	2

Table 1: Example of data representation: courses x competences x students

- *g* represents an item which in our case is a pair of a Graduating Attribute and a course
- *G<sub>a</sub>* represents the courses of student *a* (and similarly for *b*),
- *R*<sub>*a*,*g*</sub> represents the rating of student *a* for item *g* (and similarly for *b*)
- $G_a \cap G_b$  represents the common courses of students *a* and *b*,
- $\tilde{R}_a$  is the average rating of user *a*

The next step would be to find the neighbourhood of the active student which will define the set of students that will be used in order to generate predictions. Results have shown (Sarwar et al., 2000) that two techniques can effectively determine how many students will be included in the active student neighbourhood: Correlation thresholding and best nneighbours with common courses threshold (direct application of the k-nearest neighbours algorithm). In the first case, we simply select all neighbours whose absolute correlation to the active student is higher than the value of the given threshold and include them in his/her neighbourhood. In the second case, we do not simply pick the best *n* correlates, but we ask that those students selected and the active student have rated a common number of course competences (in order to guarantee that a high correlation between two students is based on a decent number of courses). In our experiments we applied Correlation Thresholding for a series of different correlation thresholds and we applied the second method (Nearest Neighbours) for different values of neighbourhood size n.

Finally, predictions for ratings is based on a weighted sum of ratings given to each item by similar students to our target student. This formula is given by Equation 3.

$$P_{m,i} = \tilde{R}_m + \frac{\sum_{j \in N_u^K(m)} sim(m,j) \cdot (R_{j,i} - \tilde{R}_j)}{\sum_{j \in N_u^K(m)} |sim(m,j)|}$$
(3)

where:

- *m* is the active student,
- *u* is the neighbourhood of students close to *m*,
- $N_{\mu}^{K}(m)$  is the K-most similar students to m
- *sim*(*m*, *j*) is provided by Equation 2,
- $R_{j,i}$  is the rating of student j on item i,
- $\tilde{R}_m$  is the mean rating of student *m*,
- $\tilde{R}_j$  is the mean rating of student *j*.

One specific characteristic of this problem (recommending courses based on ratings) is that the most recent assessment has more value. For example assuming student  $S_1$  is similar to student  $S_2$ , the rating of student  $S_2$  in the last semester is more valuable to make a recommendation based on, compared to a rating in a few semesters ago. To consider this behaviour in our algorithm we have given a higher weight to the more resent semester using a Decay function (Ding and Li, 2005; Vinagre, ). The formula for this time aware collaborative filtering algorithm is given in Equation 4.

$$P_{m,i} = \tilde{R}_m + \frac{\sum_{j \in N_u^K(m)} sim(m,j) \cdot e^{\alpha t_{R_{j,i}}} \cdot (R_{j,i} - \tilde{R}_j)}{\sum_{j \in N_u^K(m)} |sim(m,j) \cdot e^{\alpha t_{R_{j,i}}}|}$$
(4)

where:

- *t*<sub>*R*<sub>*j*,*i*</sub> represents the semester in which rating *R*<sub>*j*,*i*</sub> is given.</sub>
- $\alpha$  represents the decay parameter

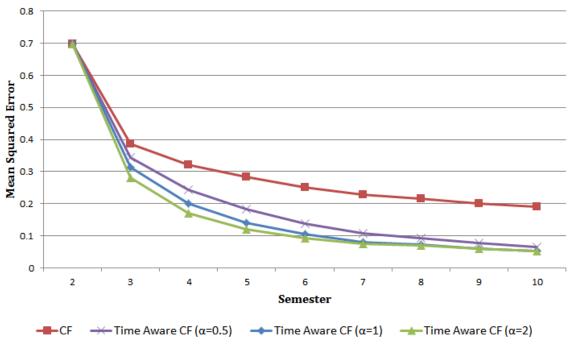


Figure 4: Mean squared error of rating predictor algorithms in each semester

#### • *e* is a constant (Euler's number)

At each semester, by having the previews ratings of students, we can predict the rating they would give to each pair (C,GA) of course and Graduating Attribute; i.e. how would the student assess the impact of a course on a Graduating Attribute. Then, we can recommend the courses with the maximum expected ratings. This recommendation can be targeted on a specific Graduating Attribute or the average of expected ratings for all the GAs.

### **4 EXPERIMENTS**

For the evaluation of the algorithm we use the synthetic data as presented in the previous Section. At each semester we can predict the ratings of students on each of the possible pairs of courses and GA for the next semester. Then we would look at the exact value of the rating in the data and calculate the mean squared error of the prediction. For the baseline we use the CF algorithm provided in Equation 3 and we compare it with the other alternative provided in Equation 4 for three different values of  $\alpha$ .

Figure 4 shows the mean square error (MSE) of the prediction at each semester. This shows that in our targeted application considering the time factor can significantly improve the results. In the results shown in Figure 4, the active user neighbourhood used for making predictions is the set of all students. By considering all the users in making the prediction we may achieve better results; however this is not an efficient method in terms of performance. As discussed in Section 3.2, there exist two techniques which can be used for determining the active user neighbourhood, Correlation thresholding and K best neighbours. In K best neighbours, for each targeted user, we rank all the other students based on their similarity, and we use the K top ones instead of all the users. In correlation thresholding, instead of having a fixed number of students, we use all the students which have a similarity to the target user higher than a specific threshold.

Figure 5 and Figure 6 show the MSE of the time aware CF algorithm using different similarity thresholds along side the percentage of users used for making the prediction. As we increase the threshold, the error of the algorithm increases but at the same time less users are used for making the prediction which makes the algorithm faster. As a result we can choose to use a threshold such as 0.7 to decrease the number of users in the active user neighbourhood with a small increase in the error.

We have performed the same experiment using K best neighbours methods. In this case instead of filtering the neighbourhood of the active user by a threshold we will choose the K most similar users. Figure 7

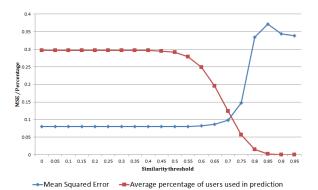


Figure 5: Results of correlation thresholding for prediction at semester 7

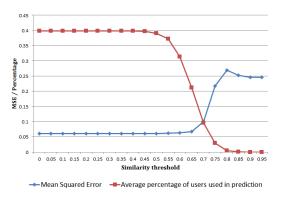


Figure 6: Results of correlation thresholding for prediction at semester 9

shows the effect of K on the MSE for the evaluation done in different semesters. The results show that the effective number of users in the neighbourhood can be between 10 to 15 students. This also matches with the result of similarity thresholding, as the threshold of 0.7 in our experiments corresponds to 30% of users, which is about 10 to 15 users (the number of students which have had common courses with target user is 30 to 50 depending on the semester). This shows that

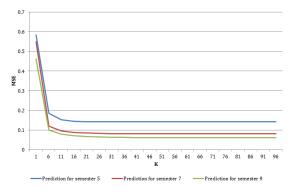


Figure 7: Results of K best neighbours method on prediction

in terms of limiting the active neighbourhood, these two methods have similar results for our application.

## 5 CONCLUSION AND FUTURE WORK

In this paper a course recommender system based on graduating attributes of students was presented. The proposed approach lies in the area of time-aware multi-criteria course recommender systems for students, which has not been attempted before in educational data mining. Experimental studies on a synthetic dataset show that time dimension of student ratings is important for more accurate recommendations and that active neighborhood of students used can be decreased significantly.

Work presented in this paper provides many avenues for further experimentation and improvement. First, experimentation on real data will bring up new challenges but also will further validate the proposed algorithm. One of the challenges is the compatibility with the program plans of the institution. For example, a recommender system should consider the prerequisites of courses in each program. Considering this issue, new options will be available for the logic of the algorithm. As an example, the algorithm may need to recommend a course which does not have a high value just to meet the prerequisites of a valuable course.

A second challenge lies with the scalability of the algorithm. To have a reasonable response time for making recommendations to a high number of students might raise the need to include new techniques. One direction to be examined would be the clustering of similar students so as to recommend courses based on clusters of similar students instead of all the dataset. Based on our results of correlation thresholding, we see that it is possible to look at a smaller set of students without sacrificing accuracy.

Finally, other collaborative filtering algorithms (like matrix factorization) will be explored, as well as explore how performance can be boosted. In the context of recommender systems an issue that should be handled is the cold start problem. One possible option for improvement is the use of content based algorithms in the fist few semesters and then over time giving more weight to the CF algorithm.

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