

## Introduction to Logical Agents

## Logical Agents

Reasoning [Ch 6]

- Why represent world? ("state information")
- Wumpus World
- Which formalism? (... logic)
- Propositional Logic [Ch 7]
- Predicate Calculus
  - Representation [Ch 8]
  - Inference [Ch 9]
- Implemented Systems [Ch 10]
- Applications [Ch 8.4,10]
- Planning [Ch 11]

## The story so far. . .

Simple situation:

- agent has to deal with SINGLE goal (Eg, get to B; clean house; ...)
- agent (designer) has accurate model of world
- agent can determine its state by sensing
- agent's actions are deterministic
- world does not change while agent is thinking
- **.**...

 ⇒ Designer only needs one "program" (Eg, heuristic function, ...)
 Agent does not need internal model of ...
 world, state, task (goal)
 Here: simple Search-based Agents are adequate

### Many situations require more. . .

World not always accessible

- ie, cannot simple "read off" state ... "perceptual aliasing"
- Reflex Agents: Keep no state information
   ⇒ Can't solve such problems

#### • State Tracking Agents:

Maintain state as a single data structure

In ambiguous situations: must use *set* of all consistent states

[Eg... unknown start state, in Vacuum World]

 $\Rightarrow$  Neither method scales up . . .

... Need (laconic) internal model to help determine best action

- Have diverse "goals"; diverse "worlds"
  - (TAXI: different destinations, different traffic patterns)
- ⇒ Need easy way to change agents (Rather than "re-programming" each time)



#### Stimulus, response! Stimulus, response! Don't you ever think?

## Knowledge-based Approach

- To be effective, agent may need to know
  - current state of the world
  - unseen properties of world
  - how world evolves
  - what it wants to achieve
  - what its actions do in various situations
- ⇒ Need to go beyond simple "Search-based Agents"
- Current Focus:
  - Deterministic
  - Discrete
  - World is Known (but state may not be)
  - Static (initially)
- Basic search techniques still used but perhaps wrt other "spaces"



## **Types of Knowledge**

- Procedural
  - e.g. functions
  - Such knowledge can only be used in one way: By executing it
- Declarative
  - e.g. constraints
  - Such knowledge can be used to perform many different sorts of inferences



#### Logic is a declarative language to:

- Assert sentences representing facts that hold in a world W (these sentences are given the value true)
- Deduce the true/false values of sentences representing other aspects of W

#### **Connect World-Representation** entail Sentences Sentences represent represent Conceptualization World W Facts Facts hold about W about W hold

#### Wumpus World!



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## **PEAS** Description

#### Performance measure

- gold +1000, death -1000
- -1 per step, -10 for using the arrow

#### Environment

- Squares adjacent to wumpus are stench-y
- Squares adjacent to pit are breeze-y
- Glitter iff gold is in the same square
- Shooting kills wumpus if you are facing it
- Shooting uses up the only arrow
- Grabbing picks up gold if in same square
- Releasing drops the gold in same square

#### • Actuators:

Left\_turn, Right\_turn, Forward, Grab, Release, Shoot

Sensors: Stench, Breeze, Glitter, Bump, Scream



Characterizing <sup>4</sup>		Ş	SSSSS Stenct		Breeze	PIT
Wumpus World				Breeze 55 5555 Stench 5 1 1 1 Gold	PIT	- Breeze -
	2	Ş	SSSSS Stench S		Breeze	
Is the world	1			Breeze	PIT	Breeze
			1	2	3	4
deterministic?	Yes					
	Outcomes specified exactly			y		
fully accessible?	No					
	Only local perception					
static?	Yes					
	Wumpus, Pits do not move					
discrete?	Yes					

### Acting + Reasoning in Wumpus World

A = Agent B = Breeze G = Glitter, Gold OK = Safe square P = Pit S = Stench V = Visited

- Wumpus

- Location: [1,1]
- Sense:
  - [-Stench, -Breeze, -Glitter, -Bump, -Scream]
- Can Reason. . .
  - As -Stench, Wumpus ∉ { [1,2], [2,1] }
  - As -Breeze, Pit ∉ { [1,2], [2,1] }
- Conclude: [1,2] is "safe"; [2,1] is "safe" ⇒ Action = Forward (to [2,1])

1,4	2,4	3,4	4,4
1,3	2,3	3,3	4,3
1,2	2,2	3,2	4,2
1,1	2,1	3,1	4,1

# Acting + Reasoning, #2

- A = Agent B = Breeze G = Gitter, Gold OK = Safe square P = Pit S = Stench
  - Visited
  - V Wumpus

- Location: [2,1]
- Sense:
  - [-Stench, +Breeze, -Glitter, -Bump, -Scream]
- Can Reason. . .



- As -Stench, Wumpus ∉ { [1,1], [3,1], [2,2] }
- As +Breeze,  $Pit \in \{ [1,1], [3,1], [2,2] \}$ Note Pit NOT in [1,1]: agent was there, did NOT fall in
- $\Rightarrow$  Only GUARANTEED safe move is...

Action = "Return to [1,1]"
 (Turn\_Left, Turn\_Left, Forward)

# Acting + Reasoning, #3

- Location: [1,2]
- Sense: [+Stench, +Breeze, -Glitter, -Bump, -Scream]
- Can Reason. . .



- As +Stench, Wumpus  $\in \{ [1,1], [1,3], [2,2] \}$
- As -Breeze, Pit ∉ { [1,1], [1,3], [2,2] }
   Note Wumpus NOT in [1,1]: agent was there, not eaten Wumpus NOT in [2,2]: else +Stench in [2,1]
- $\Rightarrow$  Wumpus is in [1,3] !
- $\Rightarrow$  Only unvisited adjacent OK square = [2,2]
- $\Rightarrow$  Action = "Go to [2,2]" (Turn Right, Forward)

## **Other Interesting Situations**



- Breeze in [1, 2], [2, 1]
  - $\Rightarrow$  no safe actions
- ⇒ Assuming pits uniformly distributed... Pit most likely in [2, 2]



- Smell in [1, 1]
  - $\Rightarrow$  cannot move
- Can use <u>coercion</u> strategy:
  - shoot straight ahead
  - Wumpus was  $[1,2] \Rightarrow dead \Rightarrow safe$
  - Wumpus wasn't there  $\Rightarrow$  in [2,1] ... safe

# Challenges

1,4	2,4	3,4	4,4
1,3	2,3	3,3	4,3
<sup>1,2</sup> S	2,2 OK	3,2	4,2
1,1 V OK	<sup>2,1</sup> B V OK	<sup>3,1</sup> P!	4,1

Need to encode what is known / observed

- + Partial information
  - Don't know where Wumpus is exactly, but constrained to  $\{\dots\}$
- + Obtained at different times, from different locations
- ... use it to reach appropriate conclusions
  - Only correct conclusions (sound)
  - All correct conclusions (complete)

#### Requires "LOGIC"

⇒ Wumpus ∈ { [1,1], [1,3], [2,2] }
 As agent was in [1,1], but not eaten
 ⇒ Wumpus NOT in [1,1]
 As -Stench in [2,1]
 ⇒ Wumpus NOT in [2,2]
 ⇒ Wumpus is in [1,3] !

As + Stench @ [1,2],

To define what answers SHOULD be returned ... Models!

### Possible Worlds ≡ Models

Initially. . .

- "PIT" in any subset of 4 x 4 grid "BREEZE" in any subset of 4 x 4 grid
  - $\Rightarrow$  so (2<sup>|{P,B,W,G,S,...}|</sup>)<sup>16</sup> possible worlds
- FOCUS: on 8 of those worlds:
  - ∃ a BREEZE in [2, 1]
  - ∃? PIT in [1, 2], [2, 2], [3, 1] ?













# Possible Worlds (II)

- KB ≡
  - Facts about WumpusWorld
  - Nothing in [1,1]
  - Breeze in [2,1]

If you believe KB, then real world  $\in M(KB)$ 



- A world does NOT match KB iff
  - $\exists$  PIT not next to a BREEZE v  $\exists$  BREEZE not next to a PIT
- 3 remaining possible worlds: M(KB)



- $\Rightarrow \alpha_1$  holds whenever KB holds!
- $\Rightarrow$  KB  $\models \alpha_1$

## Possible Worlds (IV)

- KB ≡
  - Facts about WumpusWorld
  - Nothing in [1,1]
  - Breeze in [2,1]
- α<sub>2</sub> ≡ No pit in [2,2]

•  $M(KB) \not\subseteq M(\mathcal{O}_2)$ 



⇒  $\alpha_2$  does NOT have to holds whenever KB holds! ⇒ KB  $\not\models \alpha_2$ 

## Semantics: What HAS to hold

- Given *KB*, does α have to hold?
   KB ⊨? α
- Enumerate ALL possible worlds (models)
- Use information in KB to RULE out "impossible" worlds Let M(KB) = remaining models
- $KB \models^{?} \alpha$  whenever  $\alpha$  holds in ALL models of  $KB - M(KB) \subseteq M(\alpha)$
- Why?
  - Only M(KB) are still possible
  - A holds in each of M(KB)
  - $\Rightarrow$  So  $\alpha$  must hold!
- Suggests an algorithm: "Model Checking" (later)

### Logic/Knowledge-Based Approach

- Represent knowledge as declarative statements
- Use inference / reasoning mechanism to
  - derive "new" (implicit) information
  - make decisions
- Key Problem: Need to express partial knowledge about current state
- Solution: Use intensional representation based on formal logic.
  - logical language (propositional / first-order)
  - combined w/ logical inference mechanism

- Close to human thought? -- ??
  - . . . but appears reasonable strategy for machines





## "Reasoning" Agents

#### Knowledge Base (KB) abstract data type

- Tell(KB, Fact) records Fact into KB
- Ask(KB, Query) asks whether

#### *Query* is true wrt *KB*

May return information "action" specifying when *Query* is true

```
function KB-AGENT( percept) returns an action
static: KB, a knowledge base
t, a counter, initially 0, indicating time
TELL(KB, MAKE-PERCEPT-SENTENCE( percept, t ) )
action \leftarrowASK( KB, MAKE-ACTION-QUERY(t) )
TELL(KB,MAKE-ACTION-SENTENCE(action, t ) )
t \leftarrow t + 1
return action
```

## Representing World

- Preferably:
  - expressive, concise
  - unambiguous, independent of context
  - have an effective procedure to derive implied (implicit) information
- Not easy meeting these goals . . .
  - [Halting Problem; Godel's Incompleteness. . . ]
  - ... propositional / first-order logic meet some
- Must be able to handle incompleteness / uncertainty
- Contrast with
  - programming languages
  - natural language
  - • •

### Advantages of Logic-Based Approach

#### Simply

- Store "truths"
- Ask about other (possible) truths
- Information is
  - Modular
    - Easy to build
    - Easy to modify / extend / debug
    - Capable of Explanation
  - Runnable ... to find other truths
  - Declarative:
    - Use/reuse same information to
    - Laconic
    - Introspective

Design circuit Simulate circuit Explain Circuit Diagnose Circuit