

*“The rotten tree-trunk, until the very moment when the storm-blast breaks it in two, has all the appearance of might it ever had.”*

Isaac Asimov, *Foundation*



# **CMPUT 365**

## **Introduction to RL**

# Plan

- Value Functions and Bellman Equations
  - A roadmap to the course
  - Non-comprehensive overview
  - We are still not talking about solution methods, we are only formalizing things

# Reminder

You **should be enrolled in the private session** we created in Coursera for CMPUT 365.

I **cannot** use marks from the public repository for your course marks.

You **need to check, every time**, if you are in the private session and if you are submitting quizzes and assignments to the private section.

Some students who are enrolled in Coursera **haven't submitted any quizzes or assignments** in the private session, and that's all I can see.

The deadlines in the public session **do not align** with the deadlines in Coursera.

# Plan

- Value Functions and Bellman Equations
  - Non-comprehensive overview

# Please, interrupt me at any time!



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**Chapter 2 of the textbook**  
**Week 1 of *Fundamentals of RL***



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What does “solving” a sequential decision-making problem means?
  - We need a formal language for that: MDPs.

**Chapter 3 of the textbook**  
**Weeks 2 & 3 of *Fundamentals of RL***

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**Chapter 4 of the textbook**  
**Week 4 of *Fundamentals of RL***

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**Chapter 5 of the textbook**  
**Week 2 of *Sample-based***  
***Learning Methods***

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**Chapter 6 of the textbook**  
**Weeks 3 & 4 of *Sample-based Learning Methods***



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  - We can be more efficient, we can do planning alongside learning.

**Chapter 8 of the textbook  
Week 5 of *Sample-based  
Learning Methods***

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  - We then do function approximation.

**Chapters 9 & 10 of the textbook**  
**Weeks 1, 2, & 3 of *Prediction and Control with Function Approximation***

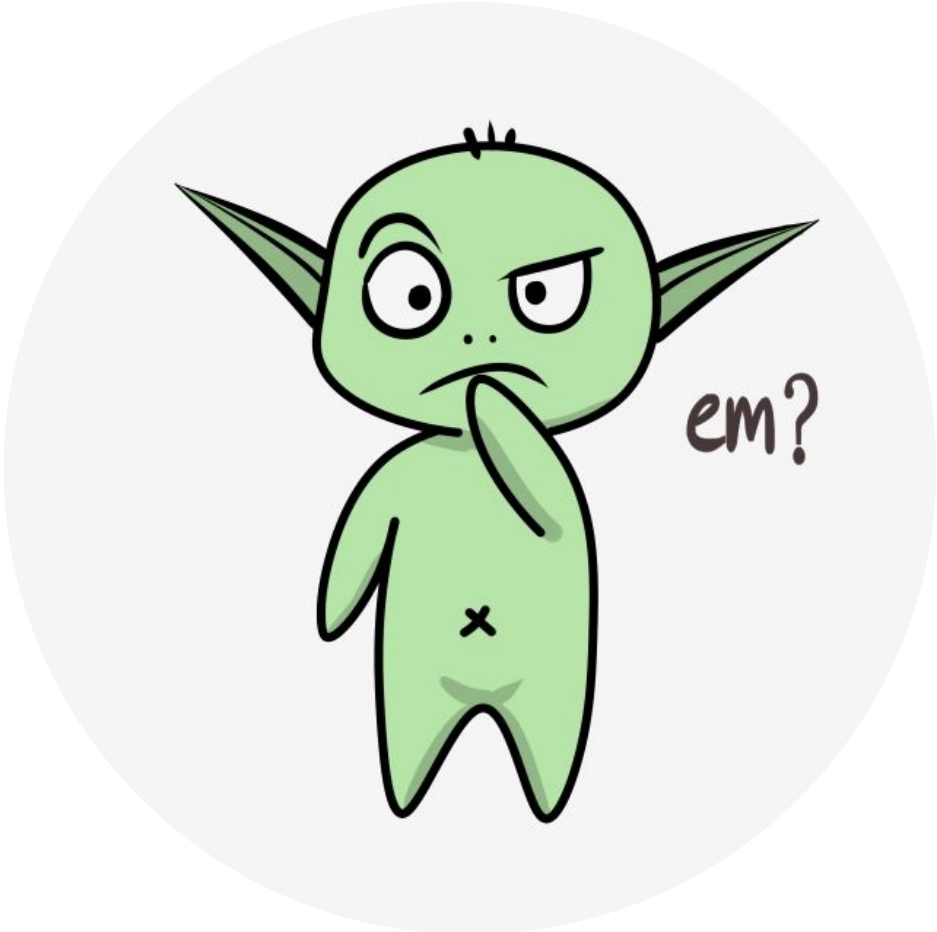
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- But what if we have many (maybe infinite) states? This doesn't scale!
  - We then do function approximation.
- What about many (maybe infinite) actions?
  - A way to tackle this problem is with policy gradient methods.

**Chapter 13 of the textbook**  
**Week 4 of *Prediction and Control***  
**with *Function Approximation***



# Value Functions and Policies

- *Value functions are “functions of states (or state-action pairs) that estimate how good it is for the agent to be in a given state”.*
- “How good” means expected return.
- Expected returns depend on how the agent behaves, that is, its *policy*.



# Policy

- A policy is a mapping from states to probabilities of selecting each possible action:

$$\pi : \mathcal{S} \rightarrow \Delta(\mathcal{A})$$

in other words,  $\pi(a|s)$  is the probability that  $A_t = a$  if  $S_t = s$ .

*Exercise 3.11* If the current state is  $S_t$ , and actions are selected according to a stochastic policy  $\pi$ , then what is the expectation of  $R_{t+1}$  in terms of  $\pi$  and the four-argument function  $p$  (3.2)? □

# Value Function

- The value function of a state  $s$  under a policy  $\pi$ , denoted  $v_\pi(s)$  is the expected return when starting in  $s$  and following  $\pi$  thereafter.

state-value  
function for  
policy  $\pi$

$$v_\pi(s) \doteq \mathbb{E}_\pi[G_t \mid S_t = s] = \mathbb{E}_\pi \left[ \sum_{k=0}^{\infty} \gamma^k R_{t+k+1} \mid S_t = s \right]$$

$$q_\pi(s, a) \doteq \mathbb{E}_\pi[G_t \mid S_t = s, A_t = a] = \mathbb{E}_\pi \left[ \sum_{k=0}^{\infty} \gamma^k R_{t+k+1} \mid S_t = s, A_t = a \right]$$

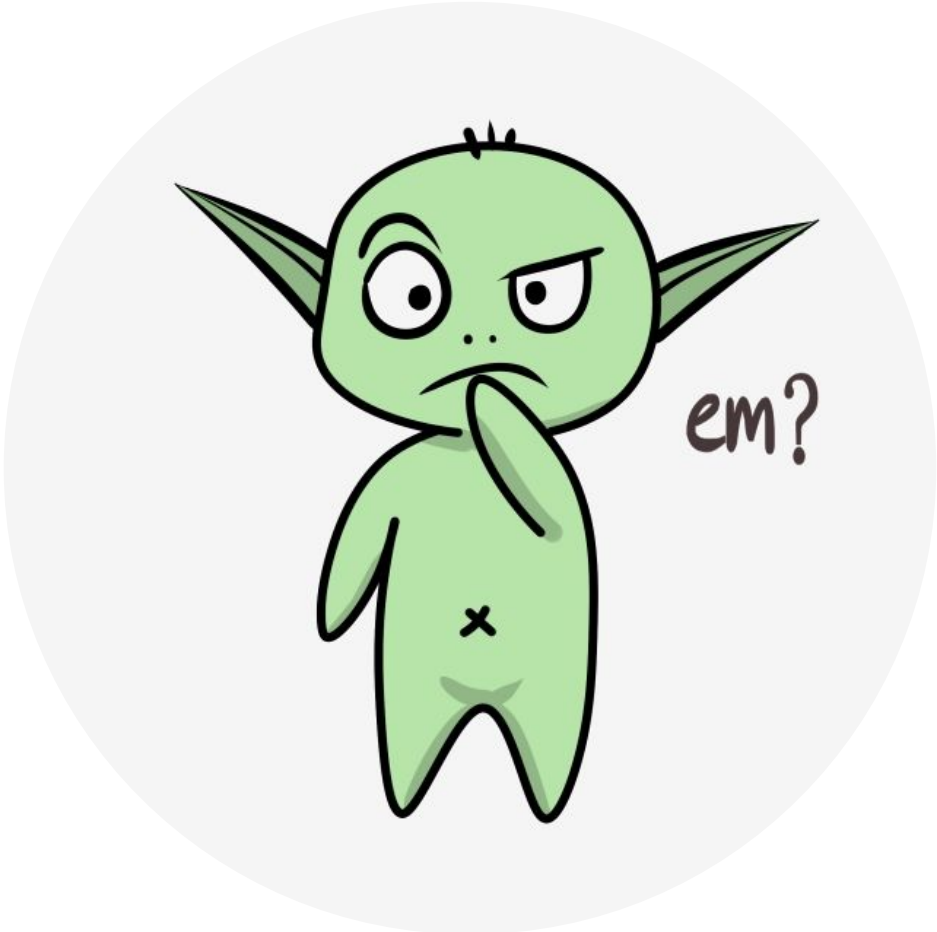
action-value  
function for  
policy  $\pi$

**Why is this difference important?**

## Exercises from the Textbook

*Exercise 3.12* Give an equation for  $v_\pi$  in terms of  $q_\pi$  and  $\pi$ .

*Exercise 3.13* Give an equation for  $q_\pi$  in terms of  $v_\pi$  and the four-argument  $p$ .



# Next class

- What I plan to do:
  - Exercises and Examples
  
- What I recommend YOU to do for next class:
  - Submit Graded Quiz for Fundamental of RL: Value functions & Bellman equations (Week 3).