

### E.g., in "input\_INTEL\_g2o.g2o"

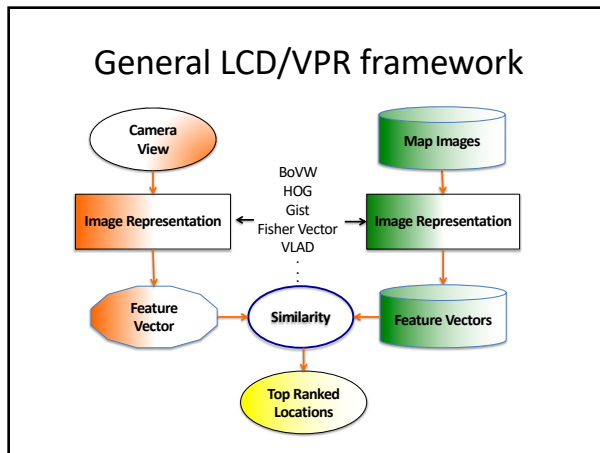
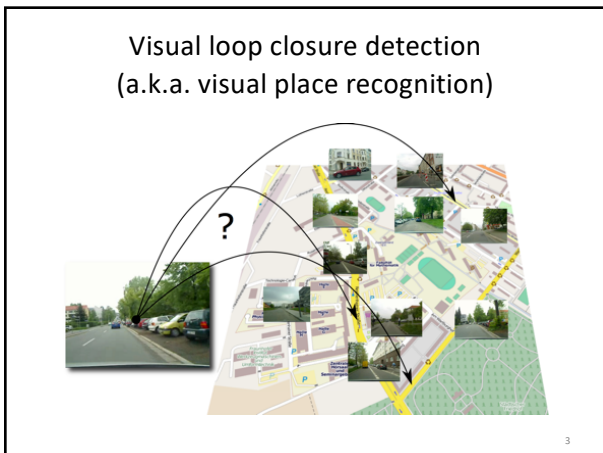
Odometric constraints: u:

```
EDGE_SE2 1224 1225 0.625700 0.003903 0.013764 11.124947 1.838454 0.000000 255.403355 0.000000 2432.575223
EDGE_SE2 1225 1226 0.106504 -0.000109 -0.016731 13.283390 -138.281257 0.000000 8813.714781 0.000000 2418.398573
EDGE_SE2 1226 1227 0.000000 0.000000 -0.000662 11.111282 -0.257444 0.000000 399.999830 0.000000 2496.693284
```

Loop closure constraints: c:

```
EDGE_SE2 19 166 -2.459689 0.241111 0.252800 11.731352 1.696454 0.000000 15.751178 0.000000 1592.856013
EDGE_SE2 19 172 -1.067903 0.915786 0.149470 22.211594 -17.729393 0.000000 39.428022 0.000000 1892.102792
EDGE_SE2 25 172 -2.539634 0.852630 -0.029860 11.348228 0.783018 0.000000 13.696833 0.000000 2357.130503
```

What are  $h_k$ ,  $\lambda_k$  and  $z_k$ ?

$$\min_{R_i, t_i} \sum_{(i,j) \in \mathcal{E}} \|\text{Log} (R_{ij}^T R_i^T R_j)\|_{\Omega_{ij}}^2 + \|\bar{t}_{ij} - R_i^T (t_j - t_i)\|_{\Omega_{ij}}^2$$


### Visual LCD/VPR

Typical LCD processing pipeline:

1. Selection of top ranked map candidates
2. Verification of the candidates (loop closure verification)

Major challenges:

1. Scalability: LCD in a map of numerous poses (images)
2. Illumination Invariance: LCD in spite of significant illumination changes between visits
3. Viewpoint invariance: LCD in spite of significant viewpoint changes between visits



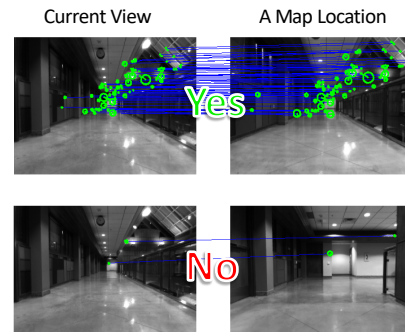
### Scalability: BoW-based solution

11. Sivic, J. and Zisserman, A. "Video Google: A Text Retrieval Approach to Object Matching in Videos", Proceedings of the International Conference on Computer Vision (ICCV), 2003.

Galvez-Lopez, Dorian, and Juan D. Tardos. "Real-time loop detection with bags of binary words." *2011 IEEE/RSJ International Conference on Intelligent Robots and Systems*. IEEE, 2011.

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### Image Matching

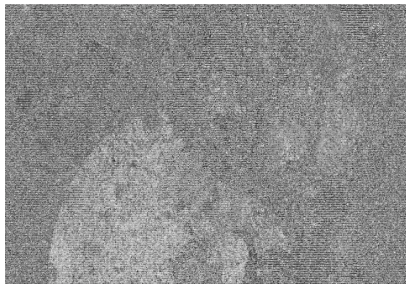


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### Image Matching?

53,000 Map Locations

Current View



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### Brute-Force Feature Matching

$$O(n^2dN)$$

$n$ : number features in an image  
 $d$ : dimension of a feature descriptor  
 $N$ : number of map locations

E.g.,  $300^2 \times 128 \times 10^5 \approx 10^{11}$

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### Bag-of-Words (BoW)

$$O(ndN/k) = O(ndN')$$

Cost of NN search for vector quantization

$n$ : number features in an image  
 $d$ : dimension of a feature descriptor  
 $N$ : number of map locations  
 $k$ : a constant scaler

E.g.,  $300 \times 128 \times 10^5 / 10^2 \approx 10^7$

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### Bag of Words?

- How does Google search the internet so quickly?
- Answer: indexing
- However, we are dealing with visual data and must express images as "text files" before indexing can be applied.

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### BoW Image Descriptor

1. Extract visual features from training images

Feature Descriptor Space (e.g., 128 dimensions)

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### BoW Image Descriptor

2. Cluster the extracted features

Training features

or dictionary:  $\{W_i\}$

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### BoW Image Descriptor

Word frequencies

Each image is described in terms of a histogram of visual word frequencies

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### BoW Inverted Index

Inverted Index

$N' = N/k$

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Slide credit: Angeli *et al.*

Dictionary

Words searching in current image

Inverted index

Score

Event  $S_t = i$

Past image indexes containing the words seen in current image

$O(ndN')$

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### Bag-of-Words w/ Vocabulary Tree

$O(nd \log[N'])$

Cost of ANN search for vector quantization

$n$ : number features in an image  
 $d$ : dimension of a feature descriptor  
 $N'$ :  $N/k$   
 $N$ : number of map locations  
 $k$ : a constant scaler

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### Bag-of-Words w/ Vocabulary Tree

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### Bag-of-Words w/ K-D Tree

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### Bag-of-Words w/ LSH

- Choose random directions
- Project visual words to these directions
- Pick a random threshold to bipartite the words

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### Bag-of-Words w/ GNNS

1. Construct a k-nearest neighbor graph (offline)
2. Randomly initialize the search (online)
3. Local hill-climbing until local minimum or a max step count is reached

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### Location/Place Recognition

Feature Match  $O(n^2dN)$

BoW

Linear Search  $O(ndN')$

Tree Search  $O(nd\log(N'))$

sGNNS Search  $< O(nd\log(N'))$

$N' = N/k$

Yes

No

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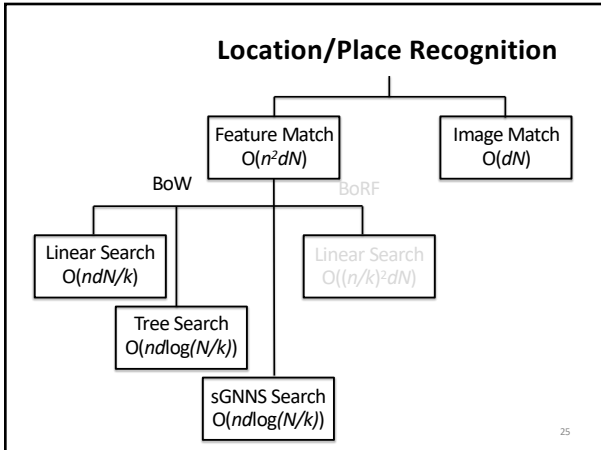
### Whole Image Descriptor

$$O(1 * dN) = O(dN)$$

$d$ : dimension of the descriptor

$N$ : number of map locations

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## Whole Image Descriptor

### $O(dN)$

Examples: Color Histogram, HOG, Gist, SIFT, SURF, Down Sampled (DS) Image, *Binarized DS Image*

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## Whole Image Descriptor

Histogram

Local histogram

Gradient based

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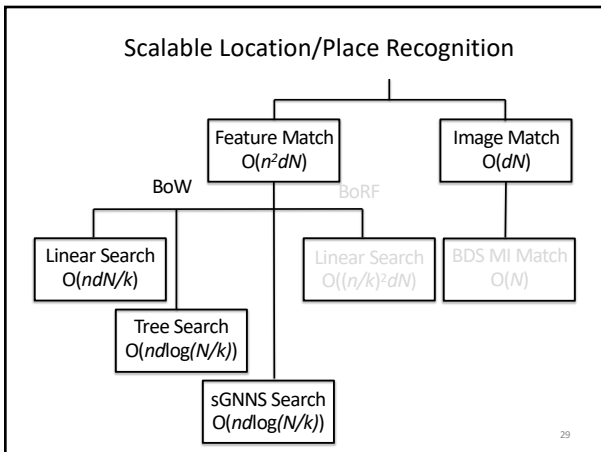
## Whole Image Descriptor

- Gabor-Gist

$d = 16 \times 20 = 320$

Yang Liu and Hong Zhang, Visual Loop Closure Detection with a Compact Image Descriptor, 2012 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS), Algarve, Portugal, October 2012

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## Summary

- Solutions to scalability
  - BoW based: sGNNS
  - Whole image based: BDS+MI
- Open issue: robustness to dynamic changes:
  - illumination
  - seasonable
  - moving objects
- Ongoing work
  - Semantics SLAM

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