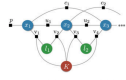


### What we will do today ..

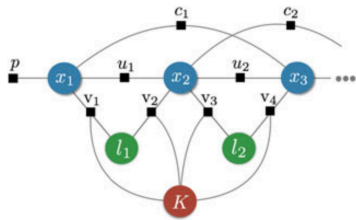


- Examples of Equation (1) in [Cadena 2016]
- Introduction to robot odometry ( $u_i$  in Fig. 3 of [Cadena 2016])
  - Coordinate frames
  - Spatial transforms (3D and 2D)
  - Wheel odometry
  - Odometry with inertial measurement unit (IMU) odometry
  - LiDAR odometry (Wednesday)
  - Visual odometry (later)
- Wednesday (9/18), we will talk about cameras and loop closure ( $c_i$ )
- Assignment No. 1, Wednesday (9/18)

### Reading Assignments

- (9/4) SLAM Survey: [Cadena 2016], pp. 1-12 (1309-1320) and pp. 17-18 (1326- 1327)
- (9/16) Basic linear algebra and coordinate transformations: <http://ais.informatik.uni-freiburg.de/teaching/ss11/robotics/slides/02-linear-algebra.ppt.pdf>
- (9/16) Mobile robot kinematics (differential drive): <http://ais.informatik.uni-freiburg.de/teaching/ss11/robotics/slides/03-locomotion.ppt.pdf>
- (9/16) RTAB-MAP: [Labbe 2019], pp. 1-12 (416-427)

### SLAM Solution



$$\mathcal{X}^* \doteq \operatorname{argmax}_{\mathcal{X}} p(\mathcal{X}|Z) = \operatorname{argmax}_{\mathcal{X}} p(Z|\mathcal{X})p(\mathcal{X}) \quad (1)$$

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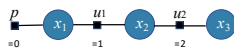
$$\mathcal{X}^* = \operatorname{argmax}_{\mathcal{X}} p(\mathcal{X}) \prod_{k=1}^m p(z_k|\mathcal{X})$$

$$= \operatorname{argmax}_{\mathcal{X}} p(\mathcal{X}) \prod_{k=1}^m p(z_k|\mathcal{X}_k) \quad (2)$$

$$p(z_k|\mathcal{X}_k) \propto \exp\left(-\frac{1}{2}\|h_k(\mathcal{X}_k) - z_k\|_{\Omega_k}^2\right) \quad (3)$$

$$\mathcal{X}^* = \operatorname{argmin}_{\mathcal{X}} -\log\left(p(\mathcal{X}) \prod_{k=1}^m p(z_k|\mathcal{X}_k)\right)$$

$$= \operatorname{argmin}_{\mathcal{X}} \sum_{k=0}^m \|h_k(\mathcal{X}_k) - z_k\|_{\Omega_k}^2 \quad (4)$$



- We can solve this toy problem by solving
- (1) a system of linear equations
  - (2) linear least square
  - (3) MLE, or
  - (4) MAP

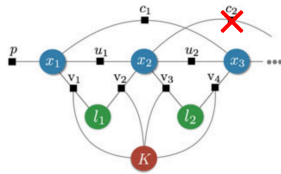


1. What is  $m$ ?
2. What are  $z_1$  through  $z_m$ ?
3. What are  $X_1$  and  $X_1$  through  $X_m$ ?
4. What are  $h_1$  through  $h_m$ ?

$$p(z_k|\mathcal{X}_k) \propto \exp\left(-\frac{1}{2}\|h_k(\mathcal{X}_k) - z_k\|_{\Omega_k}^2\right) \quad (3)$$

$$\mathcal{X}^* = \operatorname{argmin}_{\mathcal{X}} -\log\left(p(\mathcal{X}) \prod_{k=1}^m p(z_k|\mathcal{X}_k)\right)$$

$$= \operatorname{argmin}_{\mathcal{X}} \sum_{k=0}^m \|h_k(\mathcal{X}_k) - z_k\|_{\Omega_k}^2 \quad (4)$$



1. What is  $m$ ?
2. What are  $z_1$  through  $z_m$ ?
3. What are  $\mathcal{X}_i$  and  $\mathcal{X}_1$  through  $\mathcal{X}_m$ ?
4. What are  $h_1$  through  $h_m$ ?

$$\begin{aligned} \mathcal{X}^* &= \underset{\mathcal{X}}{\operatorname{argmin}} -\log \left( p(\mathcal{X}) \prod_{k=1}^m p(z_k | \mathcal{X}_k) \right) \\ &= \underset{\mathcal{X}}{\operatorname{argmin}} \sum_{k=0}^m \|h_k(\mathcal{X}_k) - z_k\|_{\Omega_k}^2 \end{aligned} \quad (4)$$

## RTAB-Map [Labbe et al. 2019]

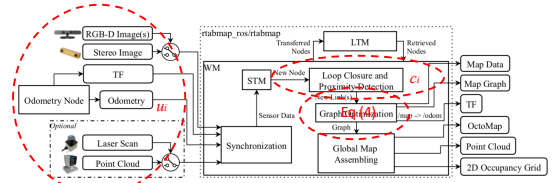


Fig. 1: Block diagram of *rtabmap* ROS node. The required inputs are: TF to define the position of the sensors in relation to the base of the robot; Odometry from any source (which can be 3DoF or 6DoF), one of the camera inputs (one or multiple RGB-D images, or a stereo image) with corresponding calibration messages. Optional inputs are either a laser scan from a 2D lidar or a point cloud from a 3D lidar. All messages from these inputs are then synchronized and passed to the graph-SLAM algorithm. The outputs are: Map Data containing the latest added node with compressed sensor data and the graph; Map Graph without any data; odometry correction published on TF; an optional OctoMap (3D occupancy grid); an optional dense Point Cloud; an optional 2D Occupancy Grid.

No w!