game of hex – two books, one puzzle

email hayward@ualberta.ca

G4G14 2022

EMAIL HAYWARD@UALBERTA.CA game of hex - two books, one puzzle

伺下 イヨト イヨト

















































hex and Gardner?

MATHEMATICAL GAMES

Concerning the game of Hex, which may be played on the tiles of the bathroom floor

by Martin Gardner

is something of an occasion these days when someone invents a mathematical game that is both new and interesting. Such a game is Hex, introduced 15 years ago at Niels Bohr's Institute for Theoretical Physics in Copenhagen. Hex may well become one of the most widely played and thoughtfully analyzed new mathematical games of the century. It swept the Scandinavian countries in the middle 1940s, and in 1949 it was taken up by game theorists in the U.S. Later Chaude E. Shannon and Edward F. Moore of the Bell Telephone Laboratories designed and built an analogue computer capable of play-

ing a moderately good game of Hex.
Hex is played on a diamond-shaped

Hex is played on a diamond-shaped board made up of hexagons [see illustrasupply of white pieces. The players alternately place one of their pieces on any one of the hexagons, provided the hexagon is not already occupied by another piece. The objective of "black" is to complete an unbroken chain of black pieces between the two sides labeled "black." "White" tries to complete a similar chain of white pieces between the sides labeled "white."

The chain may freely twist and turn, an example of a winning chain is shown in the illustration at the bottom of the page. The players continue placing their pieces until one of them has made a complete chain. The game cannot end in a draw, because one player can block the other only by completing his own chain. These rules are simple, yet Hex is a game of surprising mathematical subtlety.

Hex was invented by Piet Hem, who must surely be one of the most remark-



game of hex – two books, one puzzle



Ryan B. Hayward with Bjarne Toft



Piet Hein har konstrueret et Spil, der med lige stor Glæde kan dyrkes af Skakekaperten og den, der blot kan holde en Blyant

Vit De lære Polygon?

"Politiken" adskriver hDag en Præmieopgave, der vil volde Hovedbrud for Begyndere



ten kan alleryde Forbindainen wed at hematis det meherningende Pillt dans kanvenkoldens teron yng Bulkhermen Ecerting i dan videre Omern 1 det het Higet viser siet sig start nedvendigt at bigg ang førte 'Det af Spilletrætisking Bistogente.

26 December 4949

Eo anden Erfaring som kommer senere, mes kom pasa kan jette Spilleis Begyndelsa Vord ist reke efter itt det betaler aft få begynde i hvörr fald nogeninde pas Midten. En rimelig men pås ingen Maate nætværdig Aabning af Spillei er denne:

Paa Splindessitt i Aldem et Houlosgyndt i Midterfeltet Sam hur Sort at i Kontaktieltet ill das net mod Midtemaat Hvids Front og darved giort to nytke Felter, som staar i Vinkelsmiling in Midterfoliet, unire. Hvid har sam vagt et Felt i Kontakt med ak første. Og nu varere Sort med a besætte eV Nukelsni, agm vilde være meget nyttigt for Hvid, Hvor skal au Hvid sætler. Der av forteelling god Multgheder.

Saadan er dette Spil hui begrudt hu ken enhver tortamite. Det er altasa Hvids Turi Man skal ikke være udspekuleret fra Begruddisen. Der er ingen beker Vef fil at imre Spillet end at spille tes Det er nyttigt at se skiftevis offenskv og detensivt pas Situationen, d.v. a skiltevis pås sine egne og Modpillernes Mulaheder, for at føre en Forsöndelse igen-

EMAIL HAYWARD@UALBERTA.CA



photo credit wikipedia François Haffner

EMAIL HAYWARD@UALBERTA.CA

game of hex - two books, one puzzle



回下 くほと くほとう

1

POLYGON-SPILLEBRAT 5×5 22.1.43. Kaen J.L. Sn des myd vand, some benyf det. Det u 10 ellers ment make al lave en Me Jennem analysent (0) Opgave! I denne Ipgane begynder hid-og winder, men farst efter 15 Trak og under skadige Truster fra souls lide. "heg has proved addhillinge (men ikkes alle!) andre Mu. lighedie for builds passile Trake, min har thur dang Junder es Modrich fin contande. Vendig Hilsen. stand. may . Thaven Thashorg 1 200 game of hex – two books.

https://www.routledge.com/hex-Inside-and-Out-

◆□▶ ◆部 ▶ ◆注 ▶ ◆注 ▶ ─ 注

hex puzzle (based on Karen T) black to play



▲御▶ ▲ 陸▶ ▲ 陸▶ 三 陸



game of hex – two books, one puzzle













https://bookstore.ams.org/nml-54/

◆□▶ ◆部 ▶ ◆注 ▶ ◆注 ▶ ─ 注

bonus puzzle – black to play



イロト イヨト イヨト イヨト 三日

Michael Johanson, Yngvi Björnsson, Morgan Kan, Nathan Po, Jack van Rijswijck, Broderick Arneson, Philip Henderson, Jakub Pawlewicz, Aja Huang (AlphaGo), Kenny Young, Noah Weninger, Chao Gao, Martin Müller, Bjarne Toft, Bedir Tapkan, Md-Reza Daliri, Peter Selinger, Eric Demer, Stephen Kennedy, Bob Hearn, Nancy Blachman

イロト イポト イヨト イヨト

questions ?

email hayward@ualberta.ca

(1日) (1日) (1日)



<□ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ > < □ >



▲ロト ▲部ト ▲ヨト ▲ヨト 三国





<ロト <部ト < 注ト < 注ト = 注</p>



<ロト <部ト < 注ト < 注ト = 注</p>

WINNING 1ST-MOVES 1995 ENDERTON



<ロト <部ト <きト <きト = 3

WINNING 1ST-MOVES 2004 HBJPvR



<ロト < 回 ト < 回 ト < 回 ト - 三 三

WINNING 1ST-MOVES 2009 HAH



<ロト < 回 ト < 回 ト < 回 ト - 三 三

WINNING 1ST-MOVES 2013 AHHP



<ロト < 回 ト < 回 ト < 回 ト - 三 三

WINNING 1ST-MOVES 2014 PH



◆□▶ ◆□▶ ◆三▶ ◆三▶ ・三 ・ つへで