

Naïve Bayesian Net (NB)

- Assumption:** features are conditionally independent, given class labels
- Structure:** 1 level tree class labels — root features — leaf nodes

Input: feature vector F = (F1, F2, ..., Fn)

$$P(F|C) = \prod_{i=1}^n P(F_i|C)$$

Prediction: $class(F) = \arg \max_c P(C)P(F|C)$

$$= P(C) \prod_{i=1}^n P(F_i|C)$$

Tree Augmented Naïve Bayesian Net (TAN)

- Assumption:** allow some additional edges between features for simple correlation between the features
- Structure:** approximate the interactions among features using a tree structure among features, as well as link from class to each feature

Input: feature vector F = (F1, F2, ..., Fn)

Conditional Mutual Information between every two features F1 and F2, given C:

$$\sum_{f_1, f_2, c} P(f_1, f_2, c) \log \frac{P(f_1, f_2|c)}{P(f_1|c)P(f_2|c)}$$

Algorithm for learning structure (links between features): Chow and Liu, 1968

Prediction: $class(F) = \arg \max_c \{P(c) \prod_{i=1}^n P(f_i|c)\}$

Support Vector Machine (SVM)

- Input vectors are separated into positive vs. negative instance
- Data points that lie on the margin are "support vectors"
- Map to new feature space such as polynomial function and RBF

Perceptron: Linear separation of the input space

$h(x) = \text{sign}(\langle w, x \rangle + b)$

Artificial Neural Net (ANN)

- Practical for learning real-valued and vector-valued functions over continuous and discrete-valued features
- Robust to noise in training data
- Successful application in many other fields

Input node: feature vector F (F1, F2, ..., Fn)

Hidden node: one layer, fully connected Backpropagation algorithm

Prediction: each output node for one class

Logistic Regression (LR)

- Aims to produce smallest empirical classification error
- Gradient-descent algorithm is used to set parameters
- Learning algorithm descends in the direction of total derivative, given a set of training data

Classification Error: $Err(h) = P_{\langle e, c \rangle} (h(e) \neq c)$

Empirical Classification Error: $Err'(h) = \frac{1}{|S|} \sum_{\langle e, c \rangle \in S} (h(e) \neq c)$

Log conditional likelihood (LCL): $LCL(h) = \sum_{\langle e, c \rangle} P(e, c) \log P_h(c|e)$

Empirical LCL: $LCL'(h) = \frac{1}{|S|} \sum_{\langle e, c \rangle \in S} \log P_h(c|e)$

Logistic Regression = Discriminative Learning of NB

Learn the CPTable entries for the given NB structure to produce larger empirical LCL score, hence, smaller error

Initial CPTable: For each training data, calculate partial derivative Sum up to get a total derivative Gradient-descent algorithm to update each CPTable entry Get better conditional likelihood

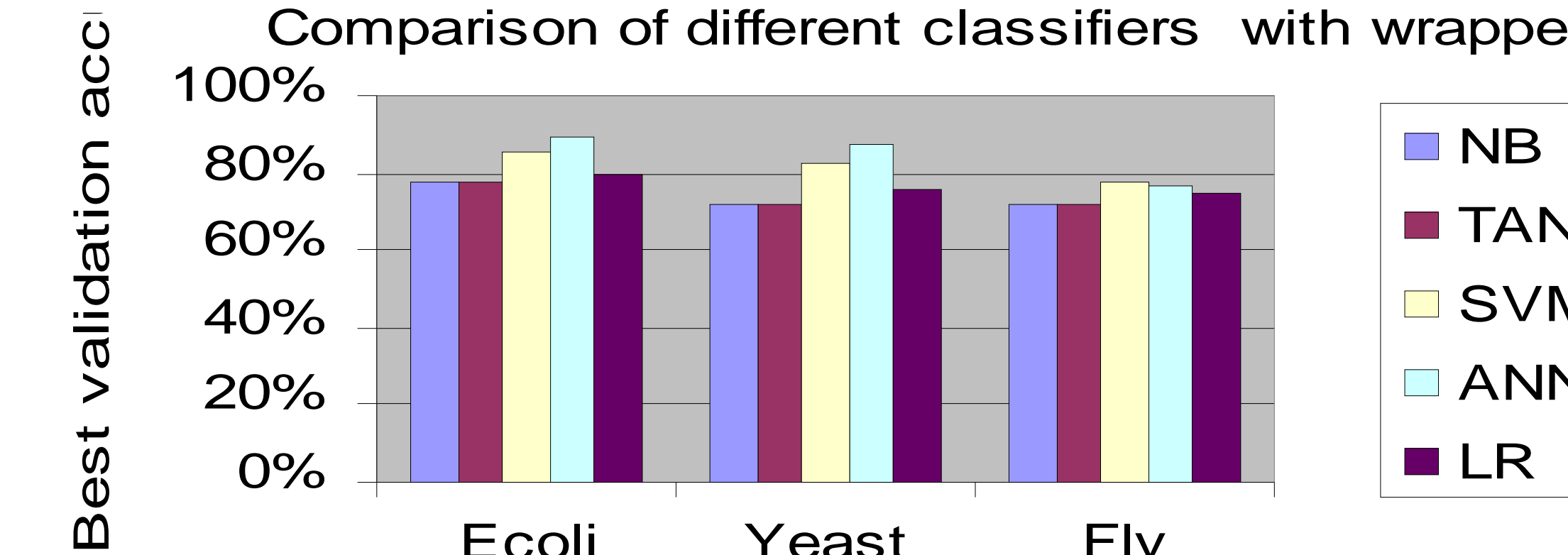
"MORE ACCURATE"!

Experiments:

- Three data sets: Ecoli, Yeast, Fly
- Evaluate each classifier using 5-fold cross validation

Results:

- Feature selection (wrapper model) improves accuracy
- ANN and SVM give best performance



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