

1. Let  $G = \text{clobber}(\text{xxxo})$ . Let  $H = \text{clobber}(\text{xxo})$ . Draw game trees for  $G$ ,  $H$ , and  $G - H$ . Which, if any, of these holds? Prove your answer.  $G = H$      $G < H$      $G > H$      $G || H$
2. Explain why  $G = 1* = 1 + *$  is equal, but not identical, to  $H = \{1 | 1\}$ .
3. For each outcome class  $\mathcal{P}$ ,  $\mathcal{N}$ ,  $\mathcal{L}$ ,  $\mathcal{R}$ , find two unequal games in that class or explain why that is not possible.
4. Let  $G$  and  $P$  be games where  $P$  is a  $P$ -position.
  - i) Assume that player  $X$  wins  $G$  as player  $t$  (1st or 2nd). Prove that player  $X$  wins  $G + P$  as player  $t$ .
  - ii) Assume that player  $Y$  wins  $G + P$  as player  $t$ . Prove that player  $Y$  wins  $G$  as player  $t$ . Hint: use i), contradiction, and no draws.
5.  $A < B$  iff \_\_\_\_\_ is a \_\_\_\_\_ position.  $B = C$  iff \_\_\_\_\_ is a \_\_\_\_\_ position.  
 Explain why  $A - B$  equals  $A - B + C - C$ .  
 Assume  $X = Y$ : explain why  $A - X + Y - Y$  equals  $A - Y$ . Hint: use previous question.  
 Assume  $A < X$  and  $X = Y$ . Prove  $A < Y$ . Hint: previous question.
6. In notation (give all left and right options), describe  $2*$ . Repeat for  $*2$ .  
 Which of  $2*$ ,  $*2$  — if either — is a number? Prove/disprove:  $*2 = *$ .
7. Give a domineering game that equals  $-1/2$ . Prove that  $-1/2 + -1/2 = -1$ .
8. Find a 5-cell domineering position equal to  $\{-1 | -1\}$ . x  
 Prove that this domineering position equals  $*$ . x x x x  
x  
x
9. Assume  $G = \{L_1 L_2 L_3 \dots | R_1 R_2 R_3 \dots\}$ . If  $L_1 < L_2$  then option \_\_\_\_\_ dominates option \_\_\_\_\_ and so  $G =$  \_\_\_\_\_ . If  $R_1 < R_2$  then option \_\_\_\_\_ dominates option \_\_\_\_\_ and so  $G =$  \_\_\_\_\_
10. Recall: for  $n \geq 1$ ,  $n = \{n - 1 | \}$ . Prove these:  $\{-3 | 16\} = 0$      $\{1 | 3\} = 2$      $\{1 | 9\} = 2$      $\{2 | 9\} = 3$