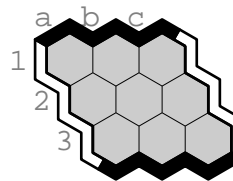


0. On page 0, in the bubbles, write your **\*\*\* CCID \*\*\***.  
On pages 0, 1, 2, 3, write your first name, last name and student id.

1. [2 marks] For a  $3 \times 3$  hex game, assume white plays first.

Circle all winning first moves.

a1   a2   a3   b1   b2   b3   c1   c2   c3



2. [3+3 marks] In github repo program `mcts1.py`, lines 2a,2b,2c below show three different ways to compute the uct value. For each choice of line 2, on my office desktop machine (used in my online lectures), I ran 20 trials of mcts on a  $4 \times 4$  hex board for 1.0 second each time.

```
1  mean_res = child.results / child.sims
```

```
2a uct = mean_res
```

```
2b uct = mean_res+(self.c*sqrt(log(self.root_node.sims)/child.sims))
```

```
2c uct = mean_res+(self.c*(self.root_node.sims/(child.sims+self.root_node.sims)))
```

- a) For each version, circle the number closest to the average number of simulations in each trial.

version 2a: 110000    130000    160000    1100    1300    1600    11000    13000    16000

version 2b: 110000    130000    160000    1100    1300    1600    11000    13000    16000

version 2c: 110000    130000    160000    1100    1300    1600    11000    13000    16000

Justify your answer briefly:

- b) For each version, out of 20 trials, give the total number of times the move returned by mcts was a winning move.

version 2a \_\_\_\_\_ /20

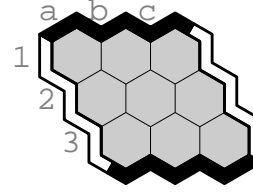
version 2b \_\_\_\_\_ /20

version 2c \_\_\_\_\_ /20

Justify your answer briefly:

3. [1+1+4+2 marks] This is a winning 3×3 hex strategy:

$$a3 \wedge (b3 \wedge (c2 \vee c3) \vee c1 \wedge (b2 \vee b1 \wedge (a1 \vee a2)))$$



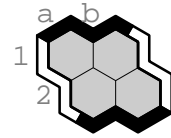
a) is this a strategy for black or for white or for both?

b) is this a first-player or second-player strategy?

c) explain the strategy in words

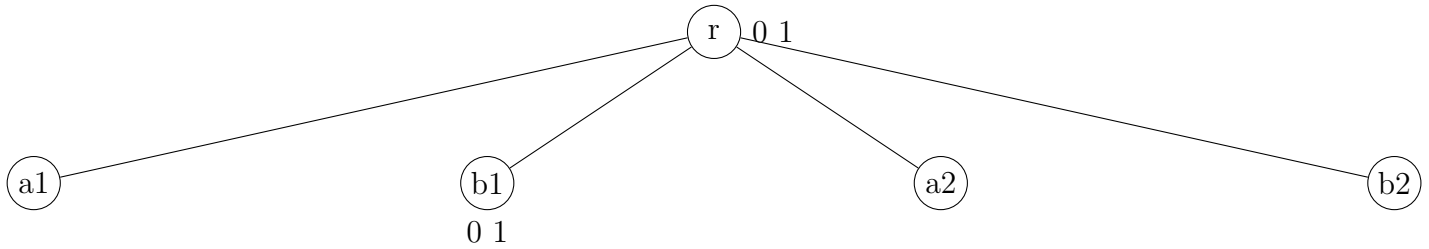
d) If you represented the strategy using a dag, how many nodes would be in the dag? Justify.

4. Here is output from an execution of the class github mcts on this hex board. Recall cells 5,6,9,10 are cells a1,b1,a2,b2. The diagram shows the search tree after sim 1. At each node, label  $x, y$  is wins,sims. Continue the diagram: show what it looks like after sim 6 (so, after all sims have executed).



```

root expand * > 5, 6, 9, 10, done
sim 1.    * 6 roll 9 5 10 parent loss
sim 2.    * 9 roll 10 6 parent win
sim 3.    * 5 roll 10 9 parent win
sim 4.    * 10 roll 6 5 9 parent loss
expand * 5 > 6, 9, 10
sim 5.    * 5 9 roll 10 6 parent win
expand * 9 > 5, 6, 10
sim 6.    * 9 5 roll 10 6 parent win
    
```



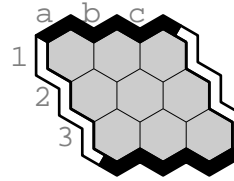
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Circle all winning first moves.

a1    b1    c1    a2    b2    c2    a3    b3    c3



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```

```
2c uct = mean_res
```

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version 2a: 16000    11000    13000    1600    1100    1300    160000    110000    130000

version 2b: 16000    11000    13000    1600    1100    1300    160000    110000    130000

version 2c: 16000    11000    13000    1600    1100    1300    160000    110000    130000

Justify your answer briefly:

b) For each version, out of 20 trials, give the total number of times the move returned by mcts was a winning move.

version 2a \_\_\_\_\_ /20

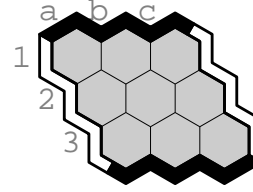
version 2b \_\_\_\_\_ /20

version 2c \_\_\_\_\_ /20

Justify your answer briefly:

3. [1+1+4+2 marks] This is a winning  $3 \times 3$  hex strategy:

$$c1 \wedge (c2 \wedge (b3 \vee c3) \vee a3 \wedge (b2 \vee a2 \wedge (a1 \vee b1)))$$



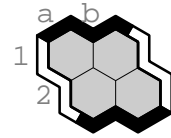
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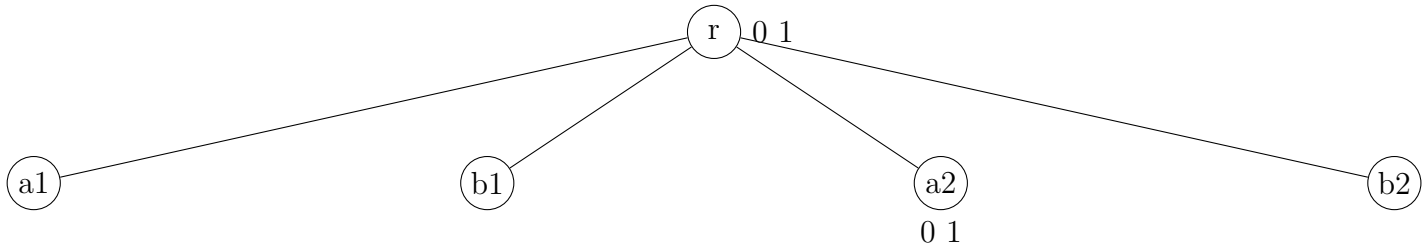
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```

root expand * > 5, 6, 9, 10, done
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expand * 6 > 5, 9, 10
sim 5.    * 6 10 roll 9 parent loss
expand * 10 > 5, 6, 9
sim 6.    * 10 9 roll 6 parent loss
    
```



first name

last name

student id

each page 8 marks

40 min

closed book

no devices

3 pages

page 1

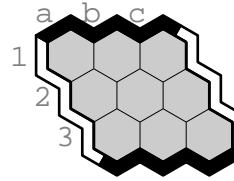
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```
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version 2c: 1300 1600 1100 13000 16000 11000 130000 160000 110000

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version 2a \_\_\_\_\_ /20

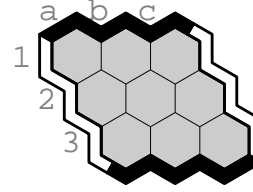
version 2b \_\_\_\_\_ /20

version 2c \_\_\_\_\_ /20

Justify your answer briefly:

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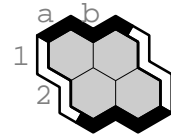
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expand * 6 > 5, 9, 10
sim 5.    * 6 10 roll 5 9 parent win
expand * 9 > 5, 6, 10
sim 6.    * 9 6 roll 5 parent loss
    
```

