

iterative Fibonacci alg'm: asymptotic analysis

- number of bits to represent n in $\Theta(\lg n)$
- addition, sum n , takes time $\Theta(\lg n)$
- $f(n)$: Fibonacci(n) $R(n)$: runtime of $\text{ifib}(n)$
- $\text{ifib}(n)$: add $f(0)$ to $f(1)$, $f(1)$ to $f(2)$, $f(2)$ to $f(3)$, ...
- create sums $f(2)$, $f(3)$, $f(4)$, ...
- $R(n)$ in $\Theta(\lg(f(2)) + \lg(f(3)) + \lg(f(4)) + \dots)$
- $R(n)$ in $\Theta(\sum_{j=2}^n \lg(f(j)))$
- Binet: $f(n) = (g^n - h^n)/\sqrt{5}$, $g = (1 + \sqrt{5})/2$, $h = (1 - \sqrt{5})/2$
- $f(n)$ in $\Theta(g^n)$
- $R(n)$ in $\Theta(\sum_{j=2}^n \lg(g^j))$
- $\lg(g^j) = j \lg(g)$
- $R(n)$ in $\Theta(\sum_{j=2}^n j \lg(g))$
- $R(n)$ in $\Theta(\sum_{j=2}^n j)$
- $\sum_{j=1}^n j = n(n-1)/2$
- $R(n)$ in $\Theta(\sum_{j=2}^n j) = \Theta(n^2)$