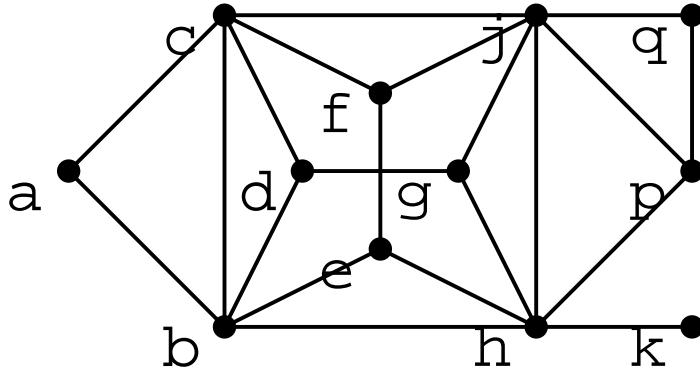


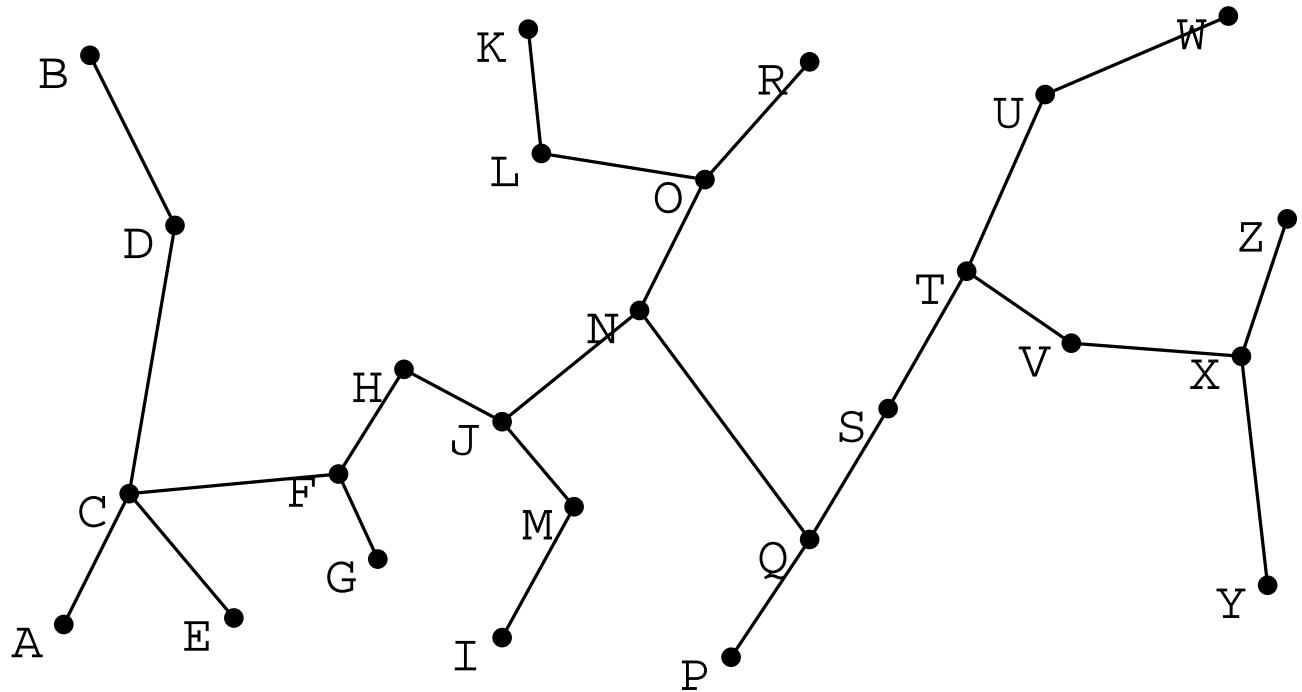
$k$ -independent set ( $k$ -IS)

- \* instance graph G
- query independent set size  $k$ ?
- \* also called max IS problem (why?)
- \* NP-complete (from  $k$ -clique)



find max IS?

- \* NP-complete :(
- \* restrict instances ?
- \* trees?     k-IS in P :)
  
- dynamic programming ?
  
- forest has isolated node (0 nbrs) or leaf (1 nbr)
  
- this works (woo hoo :)
  
- this generalizes
  
- leaf   => simplicial node: nbrhood is clique

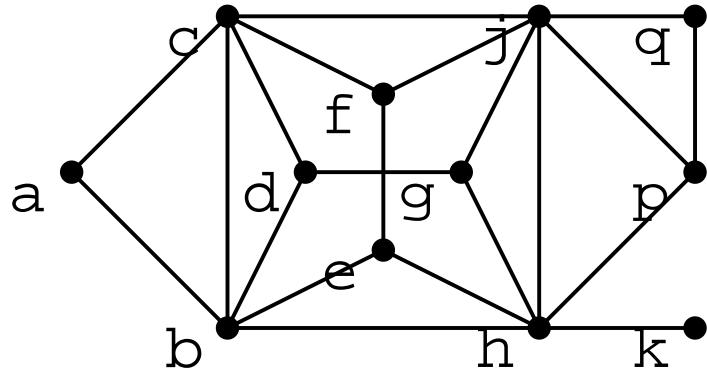


find max IS?

- \* dynamic programming ?

- \* lemma: for each leaf  $x$ ,

$$\text{maxIS}(T) = \{x\} \cup \text{maxIS}(T - x - \text{nbrhood}(x))$$

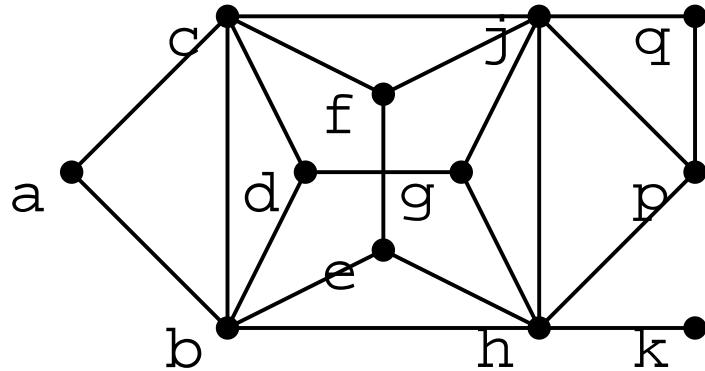


find max IS?

- \* dynamic programming ?

- \* lemma: for each simplicial node  $y$ ,

$$\text{maxIS}(T) = \{y\} \cup \text{maxIS}(T - y - \text{nbrhood}(y))$$



`dpIS(G, ISsofar)`

if G has simplicial node v:

`ISsofar <- ISsofar U {v}`

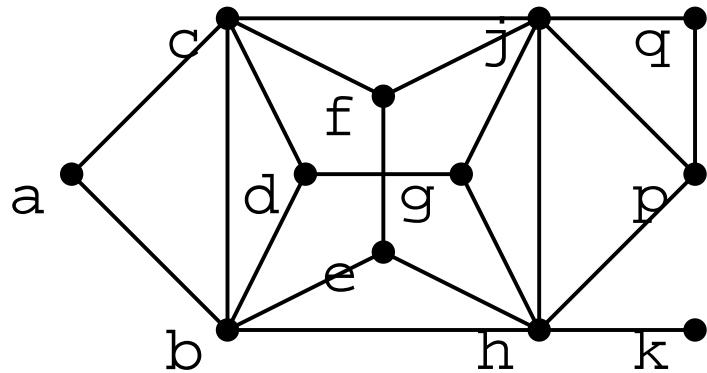
`G <- G - v - nbrhood(v)`

`return dpIS(G, ISsofar)`

return `ISsofar U bruteForceIS(G)`

`IS <- {}`

`return dpIS(G, IS)`



ISsofar

nodes

{ } a b c d e f g h j p q k

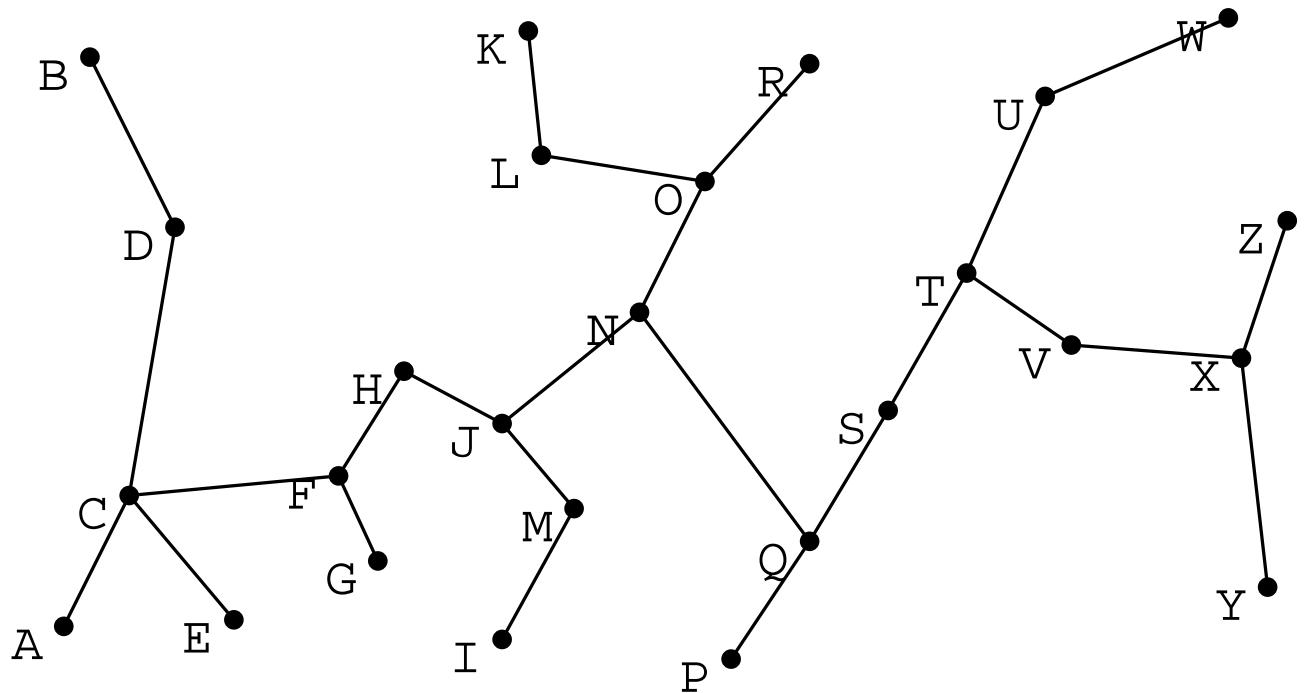
{ a } d e f g h j p q k

{ a k } d e f g j p q

{ a k q } d e f g

{ a k q d } e f

{ a k q d e }



ISsofar

nodes

{ }      a b c d e f g h i j k l m n o p q ... z

{ a }      b      d e f g h i j k l m n o p q ... z

{ a b }      e f g h i j k l m n o p q ... z

{ a b e }      f g h i j k l m n o p q ... z

...

...

