

**QUIZ 1, Jan 17<sup>th</sup> 2006, Max. marks: 10 (0.5% of final grade)**

1. What is the homogenous transformation matrix for: (5 marks)

- a) Rotation by 30 degrees around x-axis;
- b) Followed by Translate by (10, 10, -20);
- c) Followed by Rotation by 45 degrees around y-axis.

$$\text{a) } X = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos(30) & \sin(30) & 0 \\ 0 & -\sin(30) & \cos(30) & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 0 \\ 0 & \sqrt{3}/2 & 0.5 & 0 \\ 0 & -0.5 & \sqrt{3}/2 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \quad (1 \text{ mark})$$

$$\text{b) } T = \begin{pmatrix} 1 & 0 & 0 & \Delta x \\ 0 & 1 & 0 & \Delta y \\ 0 & 0 & 1 & \Delta z \\ 0 & 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 & 10 \\ 0 & 1 & 0 & 10 \\ 0 & 0 & 1 & -20 \\ 0 & 0 & 0 & 1 \end{pmatrix} \quad (1 \text{ mark})$$

$$\text{c) } Y = \begin{pmatrix} \cos(45) & 0 & \sin(45) & 0 \\ 0 & 1 & 0 & 0 \\ -\sin(45) & 0 & \cos(45) & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} = \begin{pmatrix} \sqrt{2}/2 & 0 & \sqrt{2}/2 & 0 \\ 0 & 1 & 0 & 0 \\ -\sqrt{2}/2 & 0 & \sqrt{2}/2 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \quad (1 \text{ mark})$$

The homogenous transformation matrix  $M = X * T * Y$  (2 marks)

2. What is the rotation matrix that converts the vector from the origin to  $(0, 0, 1)$  to the vector from the origin to  $(0, 1/\sqrt{2}, 1/\sqrt{2})$ ? (5 marks)

Solution 1: Rotation by 315 (or 45) degrees around x-axis.

The matrix is 
$$X = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos(315) & -\sin(315) \\ 0 & \sin(315) & \cos(315) \end{pmatrix} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1/\sqrt{2} & 1/\sqrt{2} \\ 0 & -1/\sqrt{2} & 1/\sqrt{2} \end{pmatrix}$$

Solution 2: cross product is  $(-\sqrt{2}/2, 0, 0)$ , the normalized direction is  $(-1, 0, 0)$  (A lot of people forgot to normalized the vector!), ... And you will get the same answer.

(1 mark for cross product, 2 marks for normalized cross product, 2 marks for the answer)